# Discussion on Stereovision Formulae 

Zeyu Wang

## Background

I am an undergraduate researcher of the Key Laboratory of Machine Perception, Peking University, supervised by Professor Hongbin Zha. My partners, Xiaohan Jin and Fei Xue, together with I decided to do some research on Effect Correction Based on Scene Analysis for 3D Movies. We think your paper published on IEEE Computer Graphics and Applications in 2011 is of great help.

## Prerequisites

We noticed that some formulae in A Viewer-Centric Editor for 3D Movies are different from those in A Viewer-Centric Editor for Stereoscopic Cinema, and I think that the reason may be some minor difference on definition. In the following discussion, we take A Viewer-Centric Editor for Stereoscopic Cinema as standard, regard all the coordinates as absolute values, and then try to explain these formulae.

## Discussion

Considering saving your time, I won't prove every formula here. Only what we think different from you will be proposed.
The question we are going to solve is, knowing the cinema parameters and the disparity, to calculate the 3D position that the viewer perceives.


We start from $Z_{e} . \Delta P_{e} P_{L_{-} S} P_{R_{-} S}$ is similar to $\Delta P_{e} P_{L_{-} e} P_{R_{-} e}$, thus

$$
\frac{Z_{e}-S_{z}}{Z_{e}}=\frac{P_{e} H_{S}}{P_{e} H_{e}}=\frac{P_{L_{-} S} P_{R_{-} S}}{P_{L_{-} e} P_{R_{-} e}}=\frac{d_{S}}{B_{e}}
$$

We get

$$
Z_{e}=\frac{B_{e} S_{z}}{B_{e}-d_{S}}
$$

Or

$$
Z_{e}=\frac{B_{e} S_{z}}{B_{e}-d S_{r}}
$$

Different from your

$$
Z_{e}=\frac{B_{e} S_{z}}{B_{e}-d_{S} S_{r}}
$$

Then we deal with Xe. $\Delta P_{e} P_{L_{-}} S H_{S}$ is similar to $\Delta P_{e} P_{L_{-}} H_{e}$, thus

$$
\frac{Z_{e}-S_{z}}{Z_{e}}=\frac{P_{e} H_{S}}{P_{e} H_{e}}=\frac{P_{L_{S}} H_{S}}{P_{L_{-} e} H_{e}}=\frac{P_{L_{-} S} O_{S}-M_{S} O_{S}-H_{S} M_{S}}{P_{L_{-} e} O_{e}-H_{e} O_{e}}=\frac{c_{L_{S}}-\frac{S_{w}}{2}-X_{e}}{\frac{B_{e}}{2}-X_{e}}
$$

We get

$$
X_{e}=\frac{Z_{e}}{S_{z}}\left[c_{L_{S}}-\frac{S_{w}}{2}-\frac{B_{e}}{2}\right]+\frac{B_{e}}{2}
$$

Or

$$
X_{e}=\frac{Z_{e}}{S_{z}}\left[S_{r}\left(c_{L}-\frac{W}{2}\right)-\frac{B_{e}}{2}\right]+\frac{B_{e}}{2}
$$

Different from your

$$
X_{e}=\frac{Z_{e}}{S_{z}}\left[S_{r}\left(c_{L_{S}}-\frac{W}{2}\right)-\frac{B_{e}}{2}\right]+\frac{B_{e}}{2}
$$

All symbols that appear are identical to what you defined.

| Variable name | Geometric meaning |
| :--- | :--- |
| $\left(X_{c}, Y_{c}, Z_{c}\right)$ | Real world coordinates of point P |
| $\left(X_{e}, Y_{e}, Z_{e}\right)$ | Perceived coordinates of P |
| $\mathbf{p}_{L}=\left(c_{L}, r_{L}\right)$ | Left image coordinates of P (similarly for $\left.\mathbf{p}_{R}\right)$ |
| $\mathbf{p}_{L_{S}}=\left(c_{L_{S}}, r_{L_{S}}\right)$ | Left screen coordinates of P (similarly for $\left.\mathbf{p}_{R_{S}}\right)$ |
| $B_{e}$ | Eye baseline |
| $B_{c}$ | Camera baseline |
| $d$ | Image disparity |
| $d_{S}$ | Screen disparity |
| $f_{c}$ | Camera focal length |
| $S_{z}$ | Viewer screen distance |
| $S_{w}$ | Screen width |
| $V_{c}$ | Horizontal shift (vergence) |
| $V_{c 0}$ | Original vergence position |
| $\theta_{c}$ | Camera field-of-view |
| $\theta_{c 0}$ | Original camera field-of-view |
| $\alpha_{\theta}$ | Ratio change for FOV |
| $B_{c 0}$ | Original baseline |
| $\alpha_{B}$ | Ratio change for baseline |
| $Z_{s}$ | Dolly (forward camera shift) |
| $Z_{s 0}$ | Original doll position |
| $\alpha_{Z}$ | Ratio change for dolly |

Correspondingly, $\bar{c}_{L_{S}}, \bar{c}_{R_{S}}, \bar{d}_{S}, c_{L_{S}}^{\prime}, c_{R_{S}}^{\prime}$ and $d_{S}^{\prime}$ in formula (6) and (7) are supposed to be $\bar{c}_{L}, \bar{c}_{R}, \bar{d}, c^{\prime}{ }_{L}, c^{\prime}{ }_{R}$ and $d^{\prime}$.

This is not a big problem but I am looking forward to making everything solid. Please correct me if any of my idea is wrong.

## Moreover

I sincerely hope you won't mind us taking your paper as reference. Though can't be as good as yours, we decided to realize an editing system that you proposed. We don't expect that your suggestive work provides open codes, but we do hope you can give us a software demo which we can play with. If this is still not possible, I will be grateful if you can tell us which tools you were using, for example, OpenCV, C\#, MFC, Qt etc.

I've also written a HTML only for displaying the stereovision system and its parameter effects. If you are interested, please release the RAR file attached in the same folder. Have fun!

Thanks a lot for your time and rigorousness. Forgive me if I disturbed you so many times. XD

